

1  
3 THE PROBLEM OF HINDSIGHT  
5 BIAS IN FRAUDULENT  
7 CONVEYANCE CASES: A REVIEW  
9 OF POSSIBLE “MARKET-BASED”  
11 SOLUTIONS  
13

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17

19 ABSTRACT

21 Purpose – *In fraudulent conveyance cases, plaintiffs allege that by*  
23 *entering into a complex leverage transaction, such as an LBO, a firm’s*  
25 *former owners ensured its subsequent collapse. Proving that the transac-*  
*tion rendered the firm insolvent may allow debtors (or their proxies) to*  
*claw back transfers made to former shareholders and others as part of*  
*the transaction.*

27 *Courts have recently questioned the robustness of the solvency evidence*  
29 *traditionally provided in such cases, claiming that traditional expert ana-*  
31 *lyses (e.g., a discounted flow analysis) may suffer from hindsight (and*  
*other forms of) bias, and thus not reflect an accurate view of the firm’s*  
*insolvency prospects at the time of the challenged transfers. To address*

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1 *the issue, courts have recently suggested that experts should consider*  
3 *market evidence, such as the firm's stock, bond, or credit default swap*  
5 *prices at the time of the challenged transaction. We review market-evidence-based approaches for determination of solvency in fraudulent conveyance cases.*

7 *Methodology/approach – We compare different methods of solvency determination that rely on market data. We discuss the pros and cons of these methods and illustrate the use of credit default swap spreads with a numerical example. Finally, we highlight the limitations of these methods.*

11 *Findings – If securities trade in efficient markets in which security prices quickly impound all available information, then such security prices provide an objective assessment of investors' views of the firm's future insolvency prospects at the time of challenged transfer, given contemporaneously available information. As we explain, using market data to analyze fraudulent conveyance claims or assess a firm's solvency prospects is not as straightforward as some courts argue. To do so, an expert must first pick a particular credit risk model from a host of choices which links the market evidence (or security price) to the likelihood of future default. Then, to implement his chosen model, the expert must estimate various parameter input values at the time of the alleged fraudulent transfer. In this connection, it is important to note that each credit risk model rests on particular assumptions, and there are typically several ways in which a model's key parameters may be empirically estimated. Such choices critically affect any conclusion about a firm's future default prospects as of the date of an alleged fraudulent conveyance.*

29 *Practical implications – Simply using market evidence does not necessarily eliminate the question of bias in any analysis. The reliability of a plaintiff's claims regarding fraudulent conveyance will depend on the reasonableness of the analysis used to tie the observed market evidence at the time of the alleged fraudulent transfer to default prospects of the firm.*

35 *Originality/value – There is a large body of literature in financial economics that examines the relationship between market data and the prospects of a firm's future default. However, there is surprisingly little research tying that literature to the analysis of fraudulent conveyance claims. Our paper, in part, attempts to do so. We show that while market-based methods use the information contained in market prices, this*

1 *information must be supplemented with assumptions and the conclusions*  
2 *of these methods critically depend on the assumption made.*

3 **Keywords:** Fraudulent conveyance claims; solvency determination;  
4 leveraged buyout (LBO)

## 7 9 11 **INTRODUCTION**

12 A bankrupt firm's creditors are typically paid off in a Chapter 11 bank-  
13 ruptcy according to the absolute priority rule (APR). Senior or secured  
14 creditors are paid first, with any remaining assets being used to pay unse-  
15 curred creditors. Current shareholders often receive nothing. Shareholders  
16 who sold their equity stake in the company before it went bankrupt bear  
17 no loss.

18 These rules can be overridden, however, if the company is engaged in a  
19 complex leveraging transaction, such as a leveraged buyout (LBO), before  
20 it went bankrupt. Distributions made to former shareholders may be chal-  
21 lenged by unsecured creditors as fraudulently conveyed. If the plaintiffs  
22 prevail, distributions are pulled back from the former shareholders, shifting  
23 the bankrupt firm's losses from the unsecured creditors to the former equity  
24 holders.

25 An increasing trend in fraudulent conveyance litigation is to rely on  
26 market evidence in determining whether a transaction was fraudulent to  
27 creditors, rather than other more traditional evaluative tools, such as dis-  
28 counted cash flow models. The underlying argument is that contempora-  
29 neous market evidence is more reliable than evaluations prepared by  
30 experts which may be tainted, for example, by hindsight bias.

31 This paper examines some important issues that impact the utility of  
32 using market evidence in fraudulent conveyance cases. We do not seek to  
33 resolve all such issues. Instead, our objectives are modest; we: (1) describe  
34 the key methods of analyzing credit risk that economists have developed  
35 over the past four decades, including the use of accounting ratios and prices  
36 of securities such as stocks, bonds, and credit default swaps (a type of  
37 credit derivative) as forward-looking indicators of financial distress; and (2)  
38 identify the potential strengths and weaknesses of approaches that rely on  
39 contemporaneous market data.

## 1           **LBOS AND FRAUDULENT CONVEYANCE LAW**

3   In an LBO, an investor (often a private equity firm) acquires control of a  
4   public company by buying out the firm's existing public shareholders at a  
5   premium. The private equity firm buyer typically invests some of its own  
6   capital in the transaction. However, it funds the acquisition primarily with  
7   debt (i.e., bank loans or bonds) which is collateralized by the target firm's  
8   own assets and future cash flows.<sup>1</sup> Upon completion of the LBO, the target  
9   firm is privately owned by the acquirer, and the acquired firm's capital  
10   structure consists of relatively little equity in comparison to its new debt.  
11   The benefits of such a transaction have been argued to include a new and  
12   motivated management and, in the case of a going private transaction, the  
13   ability to operate free of public disclosure requirements. Given the acquired  
14   firm's highly leveraged capital structure, however, there is potentially little  
15   room for error if plans do not go as anticipated.

16   If an LBO transaction does go poor and results in bankruptcy, the  
17   acquired firm's unsecured creditors may challenge the LBO as a fraudulent  
18   conveyance. The typical argument is that the transaction did not benefit  
19   the company, saddling the firm with onerous new debt obligations with the  
20   only beneficiary being the former shareholders and management, who often  
21   also receive payments as part of the LBO for either their stock or addi-  
22   tional compensation as a result of the transaction.

23   There are two types of fraudulent conveyances: intentional or construc-  
24   tive. Whether a company was solvent when a transfer was made (or rendered  
25   insolvent by the conveyance) is usually an issue in the subsequent  
26   lawsuit under either theory. For example, under the Bankruptcy Code, to  
27   prove an intentional fraudulent conveyance, courts often look at the com-  
28   pany's financial state at the time the transaction was being consummated.  
29   Solvency issues are even more heightened in the case of a constructive  
30   claim. To show that a transfer was constructively fraudulent, a plaintiff  
31   must show that the debtor: (1) received less than reasonably equivalent  
32   value for the transfer and (2)(a) was insolvent, or rendered insolvent, on  
33   the date the transfer was made; (b) was left with unreasonably small capi-  
34   tal; or (c) intended to incur debts beyond its ability to pay as they became  
35   due.<sup>2</sup>

36   Traditional notions of solvency are clearly at issue in item 2(a), which is  
37   typically referred to as the "balance sheet test." Specifically, Section 101  
38   (32) of the Code defines insolvency to mean a financial condition such that  
39   the sum of the entity's debts is greater than all such entity's property, at

1 “fair valuation.” Items (b) and (c) are viewed as simply being other mea-  
3 sures of the company’s financial solvency.<sup>3</sup> Test No. 2(b) focuses on  
or left with the inability to generate “sufficient profits to sustain opera-  
5 tions.” See *Moody v. Sec. Pac. Bus. Credit, Inc.*, 971 F.2d 1056, 1070  
(3d Cir. 1992) (determining whether a company is left with unreasonably  
7 small capital typically requires an analysis of the debtor’s cash flow and  
available operating capital). *In re Taubman*, 160 B.R. 964, 986 (Bankr. S.D.  
9 Ohio 1993) (noting that the phrase unreasonably small capital is not  
defined in the Code and that an appropriate analysis of the phrase involves  
11 an examination of the debtor’s cash flow and available operating capital).  
Test No. 2(c) focuses on whether the debtor intended to incur debts, or  
13 believed it would incur debts, beyond its ability to pay them. See, for exam-  
ple, *In re WLT Energy Corp.*, 282 B.R. 343 (Bankr. W.D. La. 2001) (belief  
15 to intend debts beyond the ability to pay when they matured);  
*In re EBC, Inc.*, 380 B.R. 348 (solvency existed because debtor was paying  
17 debts as they matured). Most courts, when evaluating solvency in connec-  
tion with an LBO, examine each of these three alternatives, and a case deci-  
19 sion rarely addresses only one of these items.

AU:2

## 21 THE RECENT SHIFT TO MARKET EVIDENCE IN 23 FRAUDULENT CONVEYANCE CASES

25 Solvency determinations have traditionally been made based on well-estab-  
lished evaluative tools used by experts. For instance, an expert may com-  
27 pare a firm’s debt obligations at some point in the past to the estimated  
value of its assets at the same point in time. But such historical estimated  
29 asset values are often based on an expert’s opinion about the asset’s *future*  
cash flows that were purportedly reasonable as of that historical date.  
31 Some have argued that such estimates, and consequently, the expert’s con-  
clusion about the likelihood of the firm’s imminent bankruptcy, may be  
33 tainted with hindsight bias or the expert’s perceived advocacy role.<sup>4</sup>

Two relatively recent cases [*VFB v. Campbell Soup Co.*, 482 F.3d 624  
35 (3d Cir. 2007) (“Campbell”) and *In re Iridium Operating LLC*, 333 B.R.  
283 (Bankr. S.D.N.Y.) (“Iridium”)] highlight such issues. In *Campbell*, the  
37 Third Circuit affirmed the district court’s conclusion that the value of a  
division of Campbell Soup was properly based on its market capitalization  
39 as opposed to after-the-fact valuations prepared by experts. The Third  
Circuit viewed the valuations as tainted by “hindsight bias,” *id.* at 629, and

1 complained that, to the extent the experts sought to construct a “reason-  
able valuation” of the company in light of uncertain future performance,  
3 their tools for doing so were “inapt.” *Id.* at 633.

Similarly, in *Iridium*, the court found that the experts’ conclusions on  
5 valuation lacked credibility because, among other things, the experts  
(1) ignored various financial transactions that may have impacted their  
7 conclusions, (2) did not rely on the testimony of witnesses who had knowl-  
edge of the company’s projections and the relevant capital markets at the  
9 time of the transaction, and (3) otherwise substituted their own judgments  
for those of involved parties. *Id.* at 339 42; 345 52. The court instead relied  
11 on market evidence, stating that the capital markets had “synthesized and  
distilled” what “all the smart people” knew, and that, in light of the “over-  
13 whelming weight” of the market evidence, the plaintiff could not prove  
insolvency. *Id.* at 352. To the extent the plaintiff’s expert sought to provide  
15 reasons for the company’s failure within one year of the transaction or  
otherwise prove insolvency at the time of the conveyances, the court  
17 rejected every one of the stated reasons as being tainted by hindsight or  
because the expert purportedly wrongfully discounted contemporaneous  
19 market evidence. *Id.*

However, exactly how does one infer whether a firm is solvent based on  
21 market evidence at some point in time? The three notions of solvency, the  
balance sheet insolvency, unreasonably small capital, and the inability to  
23 pay debts, are interrelated from the perspective of market evidence and all  
reflect the market’s expectations of the cash flows of the firm and of the pos-  
25 sibility of future default for the firm’s creditors. The definition of the term  
“default” depends, among other things, on the form of credit and on the spe-  
27 cific choice of the issuer’s contractual obligations to creditors that are con-  
sidered in determining whether a default event has occurred or not. For  
29 example, the future default event associated with a particular bond issued by  
a firm could refer to the firm’s failure to make coupon or principal payments  
31 in a timely manner as specified by the bond contract over the bond’s remain-  
ing maturity. In this case, what does the fact that a firm’s stock price traded  
33 at \$2 at some point in time tell us about the probability that the firm will  
default on its debt obligations over the next year, or the next two years?  
35 Similarly, what default probability estimate can be derived from the fact  
that one of the firm’s bonds traded at 75% of its face value, or its credit  
37 default swap (a type of credit derivative) traded at a particular level.

Inferring a future default probability estimate from an observed security  
39 price requires a conceptual link (an empirical or theoretical model) between  
the security price and the future default event, which may be defined in

1 different ways. We discuss some such “links” or models proposed over the  
2 past four decades in the finance literature on credit risk modeling. In addition  
3 to the observable security price, these models typically require estimates of several other economic parameters, which may be unobservable  
4 or not contemporaneously-available. That means, even when courts rely on  
5 market data to infer a future default probability estimate, such an exercise  
6 involves the use of some economic model, which in turn, requires expert  
7 analyses.<sup>5</sup> In sum, relying on market data may ameliorate but not necessarily  
8 eliminate the possible potential problems of hindsight bias in expert  
9 analyses suggested by some parties.

## 11 12 13 **A REVIEW OF CREDIT RISK MEASUREMENT** 14 **APPROACHES IN THE FINANCE LITERATURE**

### 15 *Accounting-Based Credit-Scoring Systems*

16  
17 To decide whether to make a loan, a bank considers a borrower’s ability to  
18 make the required future interest and principal payments. Decades ago,  
19 banks primarily relied on subjective borrower characteristics such as the  
20 borrower’s “4Cs” in deciding to make a loan: “Character” (reputation),  
21 “Capital” (leverage), “Capacity” (earnings volatility), and “Collateral.”  
22 Banks have discarded these measures, relying on formal *accounting based*  
23 *credit-scoring systems* which perform better (Altman & Saunders, 1998).  
24 For instance, banks now assess creditworthiness by comparing a bor-  
25 rower’s debt-to-asset ratio or his or her total interest–total income (interest  
26 coverage) ratio to an industry average. But, as Altman (2000) notes, infer-  
27 ring a firm’s financial health based on such ratios is “susceptible to faulty  
28 interpretation and ... potentially confusing” because the borrower may be  
29 superior to the industry average according to one ratio measure but inferior  
30 according to another. Therefore, more sophisticated *multivariate* models  
31 that assess a firm’s credit risk by jointly considering the impact of several  
32 key accounting ratios (weighting some more heavily than others) to calcu-  
33 late a single credit risk score or a probability of default measure, are now  
34 more commonly used.

35  
36 The most popular among such models are those that use discriminant  
37 analysis, for example, Altman’s (1968) original Z-score model, and the  
38 ZETA model developed by Altman, Haldeman, and Narayanan (1977) and  
39 Altman (2000). These models assess the financial distress of firms based on  
several variables, including the market value of equity.<sup>6</sup> Simply put, a

1 discriminant analysis identifies a *linear* function of accounting and market  
2 variables that can best distinguish between borrowers that repay versus  
3 those that do not. This requires an analysis of a set of variables to maxi-  
4 mize the between-group variance while minimizing the within-group var-  
5 iance among these variables.<sup>7</sup>

6 A final credit score depends on the weights assigned to each of these  
7 explanatory variables, which is an empirical issue. As Altman (2000) notes,  
8 “Over the years many individuals have found that a more convenient speci-  
9 fication of the model is of the form:  $Z = 1.2X_1 + 1.4X_2 + 3.3X_3 + 0.6X_4 +$   
10  $1.0X_5$ .” Use of such ratios has intuitive appeal because the accounting data  
11 necessary to compute them are generally available and the credit score can  
12 be calculated by combining these ratios using a simple linear formula.  
13 Credit-scoring models based on such ratios have performed well over dif-  
14 ferent time periods and in different countries and, at first glance, would  
15 seem well-suited to applications in fraudulent conveyance cases.  
16 Calculating a firm’s credit score at a particular point in time could arguably  
17 be accomplished without hindsight bias.

18 That said, however, discriminant models have been criticized on several  
19 grounds. The primary criticisms of such models are: (1) they are based  
20 mainly on book value accounting data which may not fully incorporate  
21 market estimates of a firm’s future prospects and may also be subject to  
22 manipulation; (2) the model’s explanatory ratios are measured as discrete  
23 time intervals and hence may not properly reflect recent changes in the bor-  
24 rower’s condition, which may be better reflected in security prices, assum-  
25 ing such securities trade in efficient markets; (3) a *linear* function of  
26 explanatory variables may be overly simplistic; and (4) such models lack a  
27 theoretical foundation and are based on empirical analysis that may be sen-  
28 sitive to the choice of variables or sample (for instance, the asset-size of the  
29 companies used in the analysis). The weights assigned to particular expla-  
30 natory variables may depend on the sample and model selected. The rela-  
31 tive importance of particular ratios may change over time and differ across  
32 firms. Hence, use of the weights from one study in a different context calls  
33 for an expert’s subjective interpretation, which may be tainted by hindsight  
34 bias, as highlighted in *Campbell and Iridium*.

35

36

### *Structural Models of Credit Risk*

37  
38  
39 With the exception of the *market value of equity/book value of total liabil-*  
*ities* ratio, none of the explanatory variables in the standard Altman

1 discriminant model directly captures the impact of possible future changes  
2 in the firm's financial condition. Instead, they are all based on a snapshot  
3 of key accounting ratios taken at particular point in time. Further, such  
4 analysis does not begin by defining what triggers default, or the fundamen-  
5 tal theoretical relationship between the selected accounting ratios and  
6 default.

7 More recent credit risk models have provided such a theoretical struc-  
8 ture by defining default explicitly, and identifying a theoretical relationship  
9 between default and particular economic variables, such as the firm's stock  
10 price or volatility of the firm's asset values. One well-known class of such  
11 "structural" models consists of the option pricing models of Black and  
12 Scholes (1973), and Merton (1974).

13 In the simplest version of such a model, a firm must make a single debt  
14 payment at some point in the future which represents the face value of a  
15 zero-coupon bond, which is assumed to be the only type of debt the firm  
16 has issued. The value of the firm's assets is assumed to change over time,  
17 obeying a specific probability distribution. Default occurs at maturity, if  
18 the value of the assets is lower than the debt's face value. In such a  
19 "default" scenario, the firm's debtholders receive the firm's assets while  
20 shareholders get nothing. Otherwise, debtholders are fully paid the pro-  
21 mised face value, and the remainder of the value of the assets is paid to  
22 shareholders as a liquidating dividend. In option-pricing parlance, the  
23 firm's equity is a call option on the firm's assets, with a strike price equal to  
24 the face value of debt. The stock's current stock price purportedly reflects  
25 the likelihood of future default.

26 To estimate the implied default probability based on the observed stock  
27 price, however, a clear conceptual link between the stock price (an observa-  
28 ble parameter) and the implied default probability (an unobservable vari-  
29 able) must be drawn. In the finance literature, several studies have drawn  
30 such a link using an option pricing model. To derive empirical estimates of  
31 default probability using such a model requires empirical estimates of the  
32 parameters which affect whether the firm's asset value will be sufficient to  
33 pay off the debt at maturity, for example, the firm's current asset value and  
34 future debt obligation, the debt's maturity, and the *volatility* of the asset's  
35 returns. Therefore, to estimate bankruptcy (or the probability of default  
36 over a particular time horizon) using an option pricing model, simply  
37 knowing the company's stock price is not enough. For example, asset vola-  
38 tility is unobservable because the firm's assets, unlike its equity (or shares)  
39 are not traded daily. Estimating the *volatility* of the firm's assets requires  
relying on an additional theoretical link which allows one to infer the

1 unobserved asset volatility level based on the observed volatility of the  
2 stock's price (or returns), provided the firm is publicly traded. Financial  
3 institutions and firms such as KMV use this approach to estimate the firm's  
4 probability of default in some future time period.<sup>8</sup>

5 Such an approach may be well-suited for use in fraudulent conveyance  
6 cases as it can be applied retroactively based on then-contemporaneous  
7 information about the firm's equity and debt values, and equity volatility.  
8 Such analyses may be less sensitive to an expert's subjective opinions.  
9 Moreover, such an analysis would include market data other than security  
10 prices and be grounded in a well-established option pricing methodology  
11 for which a Nobel prize was awarded.

12 However, despite these strengths, the approach has weaknesses too. An  
13 option pricing model-based estimate of future default probability depends  
14 critically on the model's assumptions which may not be realistic,<sup>9</sup> and on  
15 empirical estimates of parameters that are unobservable. For example, a  
16 critical parameter in such option pricing models is the volatility of the  
17 firm's asset values. As the firm's assets, which may consist of real assets  
18 such as plant and machinery and intangible assets such as patents,  
19 employee talent, and industry expertise, do not trade regularly, changes in  
20 the value of such assets (the asset's "returns"), or changes in such returns  
21 (the asset's volatility"), are generally unobservable. Further, the model  
22 assumes that the asset value changes in small increments smoothly over  
23 time.<sup>10</sup> Such a model, therefore, fails to capture sudden large changes in  
24 the asset value, which could result in default as the recent collapse of the  
25 storied investment bank, Lehman Brothers, in mid-September 2008 drama-  
26 tically illustrated. An option pricing model also generally fails to take into  
27 consideration the uncertainty associated with credit rating changes (Altman  
28 et al, 2003). Accordingly, refinements such as endogenous default and other  
29 features, have been introduced in more recent structural models.<sup>11</sup>

**AU:3**

30 The academic literature remains somewhat divided about whether struc-  
31 tural models are better at predicting default than accounting ratio-based  
32 models. According to some, structural models are better because they  
33 include historical accounting information as well as security prices that  
34 reflect investors' contemporaneous expectations about future cash flows.<sup>12</sup>  
35 Others studies refute this claim.<sup>13,14</sup> A recent study by Agarwal and Taffler  
36 (2008) finds that both approaches convey significant information about  
37 failure, but neither method subsumes the other. This result suggests that  
38 both approaches could be considered in fraudulent conveyance cases, pro-  
39 vided that the potential issues associated with both approaches (including  
40 potential hindsight bias) are properly addressed.

1 Finally, it is worth noting that another class of models use bond pricing  
2 data to assess default probabilities. Such models are referred to as  
3 “reduced-form” models because they do not explicitly model a structural  
4 relationship between default and the firm’s value. Instead such models esti-  
5 mate implied forward rates on risk-free and risky bonds and use the differ-  
6 ence in these rates to infer the market’s expectation of the risky bond’s  
7 default at different times in the future. While inferring a firm’s default pro-  
8 spect based on the market price of the firm’s debt in this way has an  
9 obvious intuitive appeal, it is important to note that bond prices also reflect  
10 a host of other economic parameters, for example, the term structure of  
11 default-free interest rates, the bond’s recovery rate given default, and time  
12 variation in the probability that a firm may default on its obligation.  
13 Consequently, models used to infer default probabilities from bond prices  
14 may rest on assumptions about parameters that may have limited empirical  
15 support.

17

*Estimating Default Probabilities using Credit Default Swap Spreads*

19

20 Market data related to credit default swaps (“CDS”) can be used as an  
21 alternative to stock or bond prices for the purpose of estimating credit risk  
22 with a structural model. Credit derivatives (such as total return swaps,  
23 spread options, and CDS) are contingent claims with payoffs that are  
24 linked to the creditworthiness of a given firm or sovereign entity.<sup>15</sup> Such  
25 derivatives have become increasingly common. For instance, the volume  
26 (measured by notional amount) of CDS first developed in 1990s peaked at  
27 \$62 trillion in 2007. Although volume declined in the aftermath of the 2007  
28 financial crisis, according to the Bank of International Settlement, the  
29 notional amount of credit default swaps outstanding in June 2014 was  
30 \$19.5 trillion.

31 The most common credit derivative is a single-name CDS, whose payoff  
32 depends on whether a defined “credit event” related to a particular refer-  
33 ence entity (country or company) occurs during the CDS’s life (typically  
34 five years). Such a credit event could be the reference entity failing to make  
35 promised interest or principal payments on a particular bond (“reference  
36 obligation”) when due, or the reference entity declaring bankruptcy (or  
37 some kind of financial restructuring).

38 A CDS, by definition, is an agreement between two parties: the buyer  
39 and the seller of the credit protection. In exchange for promising to periodi-  
cally pay the seller a fixed sum (defined as a percentage of the CDS’s

1 notional value) over the CDS's tenor, the buyer receives credit protection  
from the seller. If the credit event occurs, the seller is obliged to compensate  
3 the buyer, who may stop making payments on a going forward basis.<sup>16</sup>  
Thus, a CDS is similar to an insurance contract that the buyer holds to  
5 protect itself against loss related to a defined credit event.<sup>17</sup>

Originally, CDS contracts traded at par – that is they were designed to  
7 have a zero cost of entry, and neither the buyer nor seller was required to  
make a payment to their counterparty when the CDS contract was  
9 initiated. The fixed payment (“coupon” or “par spread”) that the buyer  
agreed to pay the seller over the life of the CDS contract was determined at  
11 the CDS contract's inception, based on the market's view of the reference  
obligation's credit risk. Over the CDS's *subsequent* life, while the coupon  
13 remained fixed, the mark-to-market value of the CDS could increase or  
decrease (from the viewpoint of the buyer) as the market's assessment of  
15 the reference obligation's credit risk changed. Thus, the market's view at  
the inception of the CDS contract about the likelihood of the default event  
17 occurring over the CDS's life can be inferred from the par spread, as we  
discuss next.<sup>18</sup>

19

21

## 22 USE OF CDS SPREADS IN FRAUDULENT 23 CONVEYANCE CASES

25 To see how CDS spreads can be used to estimate default probabilities, let  
us consider the following hypothetical example in which a CDS with a  
27 notional principal of \$1 and 3-year tenor referencing a particular bond  
issued by company XYZ is offered today at a par spread of  $S$  per annum.  
29 This means that by agreeing to pay  $S$  per year to the seller, the CDS buyer  
receives protection of up to \$1 of firm XYZ's reference debt obligation's  
31 face value.

Estimating the default probabilities over the CDS's tenor, given this  
33 market-determined spread requires several assumptions about, among  
other factors, the following: (i) the recovery rate expected upon default, (ii)  
35 the timing of the CDS spread payment the buyer must make each year, (iii)  
the timing of the default in a particular year, if default were to occur, and  
37 (iv) the “hazard rate” or the probability of default in a particular year,  
assuming default has not previously occurred.

39 The following hypothetical example clarifies how these factors are  
related and relevant in determining the relationship between the quoted

1 spread and the “market-implied” default probabilities over the life of the  
 2 CDS. In this example, we assume the following:

3

- 4 1. The recovery rate is fixed at  $RR$  percent of the underlying reference obli-  
 5 gation’s face value, that is, company’s creditors are expected to collect  
 6  $RR$  percent of the face value of debt upon default, or conversely lose  
 7  $(1 - RR)$  percent of the promised \$1 notional value if default occurs.  
 8 This is the loss for which the CDS buyer would be compensated by the  
 9 CDS seller.
- 10 2. The CDS spread is paid annually at year end up to the earlier of the  
 11 maturity of the contract or a default.
- 12 3. Default, if it were to occur, would occur at the end of the year. In that  
 13 case, the protection seller pays the buyer is  $(1 - RR)$ , which equals the  
 14 notional amount net of the recovery rate.

15

16 Let  $h$  denote the default probability (or the “hazard rate”) over a year.  
 17 It follows that the probability of surviving to the end of the first year is  
 18  $(1 - h)$ , to the end of the second year (which requires surviving the first  
 19 year) is  $(1 - h)^2$ , and the end of the third year is  $(1 - h)^3$ . The buyer must  
 20 make the first CDS payment of  $S$  at the end of the first year. The CDS pay-  
 21 ment at the end of the second year is made conditional on the reference  
 22 entity surviving the first year so its expected value is the payment of  $S$  mul-  
 23 tiplied by the probability  $(1 - h)$  that the firm survives the first year.  
 24 Similarly, the expected value of the CDS payment the buyer must make at  
 25 the end of the third year is  $S(1 - h)^2$ . The *present value* of these three  
 26 expected payments is calculated by discounting them at the risk-free rate,  
 27  $r_f$ , for one, two, and three years, respectively. The sum of the present values  
 28 of the three expected payments the CDS Buyer makes,  $P_{\text{Buyer}}$ , is:

29

$$30 \quad P_{\text{Buyer}} = \left[ \frac{1}{(1 + r_f)} + \frac{1 - h}{(1 + r_f)^2} + \frac{(1 - h)^2}{(1 + r_f)^3} \right] S$$

31

32 We next calculate the present values of the payoffs that the CDS seller is  
 33 expected to make each year over the CDS’s tenor. To do so we must calcu-  
 34 late the probability of default for *that* year. As discussed above, the proba-  
 35 bility of defaulting in *year 1* is  $h$ . The probability of surviving beyond year  
 36 1 is thus  $(1 - h)$  and the probability of surviving beyond year 2 is  $(1 - h)^2$ .  
 37 The probability of defaulting *in* year 2 is calculated as the probability of  
 38 surviving beyond year 1 minus the probability of surviving beyond year 2,  
 39

1 or  $[(1-h)-(1-h)^2]$ . Similarly, the probability of defaulting *in* year 3 is  
 2  $[(1-h)^2-(1-h)^3]$ .

3 The expected payoffs by the CDS seller at the end of the first, second,  
 4 and third years from today can be expressed as  $(1-RR)$  times the probabili-  
 5 ty of default in each of these years, that is,  $(1-RR)h$ ,  $(1-RR)[(1-h)-$   
 6  $(1-h)^2]$  and  $(1-RR)[(1-h)^2-(1-h)^3]$ , respectively. The sum of the *pre-*  
 7 *sent value* of each of these three expected payments,  $P_{\text{Seller}}$ , is:

$$8 \quad P_{\text{Seller}} = (1-RR) \left[ \frac{h}{(1+r_f)} + \frac{(1-h)-(1-h)^2}{(1+r_f)^2} + \frac{(1-h)^2-(1-h)^3}{(1+r_f)^3} \right]$$

13 If the spread  $S$  is correctly priced (i.e., properly reflects the market's view  
 14 of the hazard rate  $h$  and the recovery rate,  $RR$ ) then the  $P_{\text{Buyer}}$  must equal  
 15  $P_{\text{Seller}}$ . That is,

$$17 \quad S \left[ \frac{1}{(1+r_f)} + \frac{1-h}{(1+r_f)^2} + \frac{(1-h)^2}{(1+r_f)^3} \right]$$

$$19 \quad = (1-RR) \left[ \frac{h}{(1+r_f)} + \frac{(1-h)-(1-h)^2}{(1+r_f)^2} + \frac{(1-h)^2-(1-h)^3}{(1+r_f)^3} \right]$$

23 So, given the observed value of the spread  $S$  and the risk-free rate,  $r_f$ , to  
 24 calculate the implied hazard rate,  $h$ , one must assume a fixed value for the  
 25 recovery rate  $RR$ . Then, given the values of  $S$ ,  $RR$ , and  $r_f$ , one can solve  
 26 the equation for  $h$ .

27 For instance, if the hazard rate is 2% per annum and the risk-free rate is  
 28 5% per annum, then the sum of the present value of the CDS's buyer's  
 29 expected payments over three years (the value of square bracket term on  
 30 the *left* hand side of the above equation) is 2.6709 times the annual spread  
 31 ( $S$ ). Further assuming that recovery rate  $RR = 40\%$ , the sum of the present  
 32 value of the CDS's seller's expected payoffs, (the value of square bracket  
 33 term on the right hand side of the above equation) is 0.0321.

34 Therefore, for the implied hazard rate to be 2%, the spread  $S$  must be  
 35 such that:  $2.6709S = 0.0321$ , That is, the equilibrium spread,  $S = 0.0321/$   
 36  $2.6709$ , or 120 basis points. Conversely, if the spread is observed to be 120  
 37 basis points, then for the CDS to be correctly priced, the implied hazard  
 38 rate must be 2% per annum (assuming the recovery rate is 40% and the  
 39

1 discount rate is 5%). If the observed spread was actually higher, the  
implied hazard rate too would have to be higher, holding other parameters  
3 (such as the recovery rate) constant, assuming that the CDS contract was  
correctly priced.

5 As the preceding discussion highlights, the inferred default probability  
from CDS data depends critically on the assumptions made, for example,  
7 the timing of CDS cash flows and default.<sup>19</sup> Further, the implied hazard  
rate must be interpreted with caution. Two comments are in order. First, it  
9 represents the probability of default over a fixed period (1 year in the above  
example) conditional on the CDS default event not occurring till the start  
11 of that period, whereas the unconditional default probability over each of  
the years of the CDS's tenor is expected to change over time (and is equal  
13 to  $h$ ,  $[(1-h)-(1-h)^2]$  and  $[(1-h)^2-(1-h)^3]$  in year 1, 2, and 3, respec-  
tively). Second, as we discuss below, the probability inferred from CDS  
15 data is referred to as "risk-neutral" probability which is not the same as the  
actual default probability that investors associate with the firm's debt and  
17 in which a court may be most interested in a fraudulent conveyance case.

## 21 **LIMITATIONS TO THE USE OF MARKET-BASED** 22 **MEASURES OF DEFAULT PROBABILITIES**

23 *CDS or Bond Market Prices Yield Risk-Neutral Probability, Not Real-*  
24 *World Probability that is the Relevant Measure for Fraudulent Transfer*  
25 *Cases*

27 According to fundamental financial economics principles, the price of a  
29 security that trades in an efficient market (which incorporates all relevant  
information) must equal the present value of the security's future cash  
31 flows discounted for the delay and risk associated with such cash flows.  
For instance, consider a bond that will mature at the end of one year and  
33 has a face value of \$1 million payable at that date, unless the firm is then  
bankrupt. Assume, for simplicity, that if the firm is bankrupt the bond-  
35 holder will get nothing (i.e., the "recovery rate" is zero). If  $p$  denotes the  
probability of default, then the bondholder's expected future cash flow is  
37  $(1-p) \times \$1$  million. The present value of that expected future cash flow is  
calculated by discounting it by the rate of return investors expect to earn  
39 over the same time period (one year) if they instead invest in an equiva-  
lently risky bond. As investors are risk-averse,<sup>20</sup> this expected rate of return

1 equals the risk-free interest rate that investors can earn on a security that  
3 has negligible default risk (such as a U.S. Treasury bill) plus a risk pre-  
mium that reflects the additional return that risk-averse investors would  
5 require for investing in a risky security. For instance, if the risk-free rate of  
return is 5% and the risk premium is 10%, then risk-averse investors  
7 require 15% to invest in the bond in our hypothetical example. In turn,  
this result means that the bond's price today, or its present value, must  
9 equal its expected future cash flow,  $(1 - p) \times \$1 \text{ million}/1.15$ . If the probabili-  
ty of default,  $p$ , is 8%, the bond's current price is  $0.92 \times \$1 \text{ million}/1.15$  or  
\$800,000. That is, by investing \$800,000 in the bond today, risk-averse  
11 investors expect to earn 15% on their investment over the year, after taking  
into consideration their assessment of the probability that the bond may  
13 default (in which case they would lose their entire investment). Conversely,  
if we observe the bond with a stated face value of \$1 million, trading for  
15 \$800,000 and we know that risk-averse investors require a risk premium of  
10% over the risk-free rate of 5% to make such an investment, we can infer,  
17 based on such market data, that the bond's default probability is assessed  
to be 8% by risk-averse investors.

19 In practice, such an inference may be difficult to draw because of the dif-  
ficulty in accurately estimating the risk premium that risk-averse investors  
21 require. There is, however, a technique known as "risk-neutral" valuation  
in valuing derivatives (securities whose values are linked to that of another,  
23 more primitive security, e.g., a call option written on a stock, or a CDS  
contract that references a bond) that allows for the issue to be circum-  
25 vented. This technique relies on the key insight that as long as investors  
can buy or sell either the derivative or the underlying security and a  
27 risk-free bond freely, then the arbitrage-free price of the derivative can be  
measured relative to the price of the primitive security (which presumably  
29 properly captures investors' degree of risk-aversion as discussed above).<sup>21</sup>  
As a result, in pricing the derivative further consideration of investors' risk-  
31 aversion is irrelevant. Therefore, for mathematical convenience, the deriva-  
tive can be priced assuming that investors are risk-neutral and do not  
33 require any risk premium above the risk-free rate to invest in the risky deri-  
vative (as opposed to real-world risk-averse investors) but assign a proba-  
35 bility of default, called *risk-neutral probability* of default, that differs from  
the real-world default probability assigned by risk-averse investors. As the  
37 risk-free rate is publicly observable, this considerably simplifies the calcula-  
tion to infer the bond's *risk-neutral* probability of default. For instance, in  
39 the preceding example, if the bond trades at \$800,000, and the risk-free rate  
of return is 5%, this means that risk-neutral investors expect to earn  $1.05 \times$

1 \$800,000 or \$0.84 million by the end of the year. As the face value of the  
 2 bond is \$1 million (and assuming the recovery rate to be zero as before)  
 3 this means that risk-neutral investors assign a 16% *risk-neutral* probability  
 4 of default to the bond,<sup>22</sup> whereas the actual probability of default is  
 5 assumed to be only 8%.

6 As the conceptual risk-neutral probability of default may be higher than  
 7 actual default probability in which the court in a fraudulent conveyance  
 8 case would be interested, the exact relationship between risk-neutral and  
 9 actual default probabilities must be empirically estimated.<sup>23</sup> For instance,  
 10 using U.S. corporate bond price data (rather than CDS data), Driessen  
 11 (2005) estimated the average ratio of risk-neutral to actual default intensi-  
 12 ties to be 1.89, that is, actual default probability was estimated to be about  
 13 half its risk-neutral counterpart.<sup>24</sup> In contrast, using CDS data, Berndt  
 14 et al. (2008) estimated the median ratio of risk-neutral to actual default  
 15 probabilities for broadcasting-and-entertainment firms. The study found  
 16 that the median ratio (a) climbed to above 8 in the third quarter of 2002,  
 17 before dropping to below 4 by December 2004 *for five-year maturities*; and  
 18 (b) peaked at 8 in the third quarter of 2002, dropping to 1 by December  
 19 2004 *for one-year maturities*.<sup>25</sup> Thus, the estimated relationship between  
 20 risk-neutral and actual default probabilities varies significantly over time,  
 21 and by the maturity considered, even if the sample of firms considered and  
 22 the methodology used for the estimation remains unchanged.

23 More generally, the above discussion highlights a conceptual issue,  
 24 namely that the price of a risky bond (or a CDS on such a bond) reflects  
 25 three influences: the bond's default probability, a recovery rate and the  
 26 investors' risk premium. For instance, the expected future cash flow of a  
 27 one-period bond with a face value of \$1 million equals  $(1 - p) \times \$1 \text{ million}$   
 28  $+ p \times RR \times \$1 \text{ million}$ , where  $p$  represents the actual probability of default,  
 29 and  $RR$  the recovery rate (which we previously assumed was zero). The  
 30 bond's present value equals:

31

$$32 \quad p_0^B = \frac{[(1 - p) + p(RR)]\$1 \text{ million}}{[(1 + (r_f + RP))]}$$

35

36 where  $r_f$  and  $RP$  denote the risk-free rate and the risk premium,  
 37 respectively.

38 It follows that an increase in the probability of default or the risk pre-  
 39 mium would result in a decline in the bond's present value or price, while  
 an increase in the recovery rate would have the opposite effect, holding

1 other factors constant. Thus, a decline in bond's price could be due to one  
3 or some combination of the following reasons: (1) an increase in risk-averse  
5 investors' assessment of the bond's default probability, (2) a decrease in  
7 investors' assessment of the bond's default recovery rate upon default, or  
9 (3) an increase in the risk premium. Hence, any attempt to infer the extent  
11 to which investors revised their probability of default assessment at the  
time of an alleged fraudulent conveyance based on observed changes in  
bond (or CDS) prices must consider, and control if necessary, for any por-  
tion of the observed price change attributable to the other two factors (con-  
temporaneous changes in the risk premium and recovery rate). This may be  
a difficult task.

13

*CDS Spreads Reflect Counterparty Risk (among Other Factors) which Is  
15 Not Relevant to the Probability of Default Measure Relevant in Fraudulent  
Transfer Cases*

17

The protection offered by a credit default swap is only as good as the pro-  
19 tection seller's ability to honor its commitment if the credit event occurs.  
This counterparty risk affects the pricing of CDS contracts. Dealers with  
21 higher credit risk charge lower spreads for the same CDS contract com-  
pared to other dealers.<sup>26</sup> Such counterparty risk is irrelevant in the context  
23 of fraudulent conveyance actions in which courts are interested in the likeli-  
hood of default by the debt issuer, not that of an insurer of such debt (i.e.,  
25 the CDS seller). Therefore, a market-based default probability derived  
from CDS spreads must be adjusted for such counterparty risk associated  
27 with the dealer offering the contract, or other factors also unrelated to the  
issuer's probability of default, such as tax effects and liquidity.<sup>27</sup> Such fac-  
29 tors, which are unrelated to the default probability, may explain differences  
in the same CDS contract's spread posted by different dealers.<sup>28</sup>

31

*The Default Probability Inferred from One CDS Spread May Be  
33 Inappropriate to Assess the Probability of Default for the Class of Debt  
35 Claims at Issue in A Fraudulent Transfer Case*

37 Courts may often be interested in evaluating how a particular transfer  
impacts the solvency of a particular creditor or class of creditors. However,  
39 there may be several credit default swaps referencing different classes of  
debt issued by the same entity (say, a bank). The December 2014 SRO

1 Published List<sup>29</sup> issued by MarkitSERV, which processes the majority of  
credit derivative products available to trade today,<sup>30</sup> identifies two classes  
3 of standardized CDS contracts<sup>31</sup> for several reference entities or firms.<sup>32</sup>  
For example, MarkitSERV identified HSBC's senior bond (with a coupon  
5 rate of 3.75%, maturing November 30, 2016; ISIN: XS0470370932) as the  
Standard Reference Obligation (SRO) for all standard CDS contracts that  
7 reference HSBC Bank "senior unsecured" debt. Similarly, MarkitSERV  
identified another HSBC subordinate bond (ISIN: XS0114072423), that  
9 pays no coupon interest and matures on July 21, 2020, as the SRO for all  
standard CDS contracts that reference HSBC Bank "subordinate" debt.

11 Note, however, that HSBC currently has over 1,400 different debt secu-  
rities outstanding. Using the default probability implied by the CDS spread  
13 which references a particular HSBC bond would clearly not be an appro-  
priate measure of the default risk for other HSBC debt claims which may  
15 have different payoff priority in the event of default. Therefore, the court  
in a fraudulent conveyance matter should recognize the potential for error  
17 that may arise in relying on the default measure implied by any CDS  
spread, given differences in seniority between the CDS' reference obligation  
19 and the debt claims at issue in the case.

Two further comments are in order. First, MarkitSERV's SRO Published  
21 List does not identify an SRO for all reference entities. For instance, the list  
only identifies a senior SRO for ING Bank. The default probability implied  
23 by that CDS spread would clearly not be an appropriate measure of the  
default risk for subordinate debt claims against ING Bank. Second, the SRO  
25 Published List only covers 88 reference entities at the time of this writing even  
though CDS contracts related to other firms' debt may be traded through  
27 MarkitSERV. In such cases, CDS counterparties are free to choose the CDS  
contract's reference obligation from a small list provided by MarkitSERV.<sup>33</sup>  
29 Once again, the default probability implied by a CDS spread related to some  
Bank of America bond does not necessarily serve as an appropriate measure  
31 of the default risk for other debt claims against the bank. For example, Bank  
of America has over 1,036 debt securities outstanding, including \$8.7 billion  
33 *junior* subordinated debt obligations outstanding as of January 2015. Such  
claims have lower priority than the bank's senior, or even its subordinated  
35 debt, in the event of default.<sup>34</sup> Therefore, the default probability implied by a  
CDS spread related to any Bank of America CDS contract (referencing either  
37 its senior or subordinated debt) would under-estimate the default risk for  
such *junior* subordinated debt.

39 Further, the SRO identified for a CDS contract may be subsequently  
substituted if its maturity declines to less than a critical threshold (six

1 months to one year). Hence, the default probability inferred from an  
observed CDS spread may reflect not just the existing SRO's default likeli-  
3 hood but also that of future substitute SROs.<sup>35</sup>

5

7

## CONCLUSION

9 Market prices of shares, bonds, and credit default swaps reflect default  
probability expectations so, in principle, any of these securities' market  
11 prices can be used to infer the probability of default that investors assigned  
to a particular firm at a particular point in time. Courts have expressed the  
13 opinion that such market-based approaches may be more objective com-  
pared to ones typically preferred by plaintiffs' experts in fraudulent convey-  
15 ance actions that may reflect hindsight bias and other identified issues.  
However, courts should recognize that deriving such a market-based  
17 default probability raises several methodological and conceptual questions.  
In this paper, we summarize some of the well-known methods of inferring  
19 probability of default from security prices developed in the finance litera-  
ture over the past several decades and the issues associated with such  
21 methods.

As noted above, in addition to default probability expectations, security  
23 prices also reflect information about a host of other value-relevant factors  
such as tax effects, liquidity, and counterparty risk which may not be rele-  
25 vant in a fraudulent conveyance case. Therefore, to infer the default prob-  
ability per se, using a security's price, adjustments for the impact of such  
27 other value-relevant factors on that security's price may be necessary.

Inferring a default probability from equity prices (which are available  
29 only for publicly traded firms) requires the use of some model (such as the  
option pricing model), which in turn involves assumptions and parameter  
31 inputs that are difficult to estimate empirically. The probability of default  
inferred from CDS premiums, reflects a theoretical *risk-neutral* probability  
33 that may be several times higher than the *actual* probability of default  
which is the relevant measure that courts require in fraudulent conveyance  
35 cases. Transforming risk-neutral probabilities to actual default probabilities  
is an empirical exercise and the relationship between these two measures  
37 can vary widely over time, across industry and by the tenor of the CDS  
instrument selected for the analysis.

39 Finally, different CDS contracts reference different classes of debt issued  
by the same firm. Therefore, the probability of default inferred for one class

1 of debt from a CDS contract's spread may over- or under-estimate the  
3 default probability of other classes of debt by the firm which may at issue  
in a fraudulent conveyance case.

5 In short, there are multiple approaches to assess investors' assessment of  
the probability of future default by a firm based on market prices. Such  
7 market-based approaches may help alleviate the alleged hindsight bias  
associated with expert opinions in fraudulent conveyance cases, as some  
9 courts have noted. However, deriving such market-based default estimates  
also entails models, assumptions, and empirical estimates of unobservable  
11 parameters that require the use of experts. Different experts, using the  
same market data (but different models and parameter values and assump-  
13 tions), could thus reach widely different conclusions about the probability  
of default associated with a particular firm at some point in time in the  
15 past. Courts should thus recognize that an expert's opinion about a firm's  
likelihood of going bankrupt following an allegedly fraudulent transfer  
17 that is based on market evidence may remain subject to many of the same  
concerns expressed by the *Campbell* and *Iridium* courts.

19

## 21 NOTES

21

23 1. <http://www.nasdaq.com/investing/glossary/l/leveraged-buyout>

23

2. See Simkovic and Kaminetzky (2011).

25

3. The concept of solvency found in item 2(a) itself may raise a concern. A  
25 firm's debt and asset values at a particular point in time do not necessarily inform  
one about when (if ever) the firm would go bankrupt. Even if the firm's asset values  
27 exceeded that of its debt at a point in time, the firm may eventually default on some  
debt payment. The converse is also true. Even if the book value of a firm's assets is  
29 lower than its debt, it does not mean that the firm will certainly default on its debt  
in the future. Market evidence can be useful in such situations. If a firm's securities  
31 trade in an informationally "efficient" market (in which security prices such as the  
firm's stock or bond prices reflect all relevant contemporaneously-available infor-  
33 mation), then one may be able to infer investors' assessment of the likelihood of  
future default by the firm at the time using such security prices. Such an estimate  
would be based on information that was available to investors at the time, and thus  
not tainted with hindsight bias.

35

4. Simkovic and Kaminetzky (2011).

37

5. Moreover, once a default probability is derived based on historical market  
data, a fact-finder would have to ascertain whether the default probability was suffi-  
37 ciently high to render a particular transaction "fraudulent." To our knowledge,  
such parameters are not firmly developed in the case law.

39

6. See Altman (1968), Altman et al. (1977), and Altman (2000).

1       7. The following five explanatory variables for predicting financial distress are  
included in the model in Altman (2000):

- 3       (1) Working Capital/Total Assets – measuring the firm’s “net liquid  
assets ... relative to the total capitalization”;
- 5       (2) Retained earnings/total assets – measuring “total amount of reinvested earn-  
ings and/or losses of a firm over its entire life” relative to its total capitalization;
- 7       (3) Earnings before interest and taxes/total assets – measuring the “true productiv-  
ity of the firm’s assets, independent of any tax or leverage factors”;
- 9       (4) *Market value* equity/book value of total liabilities – measuring how much the  
firm’s assets can decline in value (measured by market value of equity plus debt)  
before the liabilities exceed the assets and the firm becomes insolvent”; and
- 11      (5) Sales/total assets or capital-turnover ratio – measuring the “sales generating  
ability of the firm’s assets” and reflects “management’s capacity in dealing with  
13      competitive conditions.”

15      8. More precisely, KMV empirically estimates a “distance from default” mea-  
sure based on the number of standard deviations by which the firm’s asset values  
17      currently exceeds its outstanding debt obligations, and the percent of firms that  
actually went bankrupt within one year that also had asset values that exceeded  
their debt obligations by the same number of standard deviations (Altman &  
Saunders, 1998). KMV was acquired by Moody’s in 2002.

19      9. For instance, the model assumes that the firm has a single class of debt which  
can default only at maturity, not earlier. To instead incorporate multiple classes of  
21      debt, the priority of each debt class in bankruptcy must be specified. Further, as  
Franks and Torous (1994) discuss, such priority rules may not be followed upon  
23      default. Default may not be exogenous as the model discussed above assumes.  
Instead, if default entails a cost (a fraction of the firm value that is lost when default  
25      occurs), in order to maximize shareholder value, management may optimally choose  
when to default.

27      10. That is, such option pricing models generally assume that the firm’s value “is  
continuous in time” and therefore “time of default can be predicted just before it  
happens,” that is, there are no “sudden surprises.” Further, the Merton model also  
29      assumes that the firm’s assets future returns are lognormally distributed; a technical  
assumption that tends to overstate recovery rates (compared to a model in which  
the asset returns are assumed to obey a “more fat tailed distribution” (Altman,  
31      Resti, & Sironi, 2003).

33      11. According to Leland (2004), structural models with endogenous default  
boundary or appropriately chosen exogenous default boundary predict the general  
shape and level of default probabilities for A, Baa, and B rated debt quite well for  
horizons exceeding 5 years.

35      12. See Hillegeist, Keating, Cram, and Lundstedt (2004). Kealhofer (2003) and  
Oderda, Dacorogna, and Jung (2003) also find that structural models outperform  
37      credit ratings.

39      13. See Reisz and Perlich (2004). Campbell et al. (2006) find such market-based  
models have little forecasting power after controlling for other variables.

14. This could occur if accounting information incorporated into accounting-  
based models is incrementally informative over stock and bond prices. This could

1 happen if asset values are difficult to assess and if debt covenants are based on  
accounting information. See Core and Schrand (1999) and Duffie and Lando  
3 (2001).

5 15. The description of credit derivatives and credit default swaps is based on  
Longstaff, Mithal, and Neis (2005).

7 16. If the CDS is physically settled, the protection seller agrees to buy the refer-  
ence issue at its face value from the protection buyer in the event of a default by the  
9 reference entity. If the CDS is cash settled, the protection seller agrees to pay to the  
protection buyer cash equal to the difference between the notional value and the  
market value of the reference obligation following a credit event. This market value  
is determined through auction in a predetermined manner.

11 17. The protection buyer in a CDS contract faces the risk that the protection  
seller will not honor its CDS obligations in case of a credit event. To reduce this  
risk, the CDS contract may require the protection seller to post collateral. The  
13 details of the collateral requirement are specified in the ISDA Master agreement  
associated with the CDS contract. The collateral amount is usually contingent on  
the credit rating of the protection seller. A highly rated protection seller may not  
15 need to provide any collateral but the collateral amount increases as the rating of  
the protection seller falls.

17 18. Following the credit crisis, in 2009, ISDA issued the “Big Bang” protocol to  
standardize CDS contracts and increase the liquidity of such derivatives (Markit,  
2009). Now the standardized coupon for all North American CDS contracts is  
19 either 1% or 5% (100 or 500 basis points), regardless of the market’s view of the  
underlying reference obligation’s credit risk at the time the CDS contract is initial-  
21 ized. The market’s view of such risk, which used to be captured by the spread  
before Big Bang, is now captured in an up-front charge (known as the “Points Up-  
23 Front (PUF),” quoted as a percentage of the notional), which the protection buyer  
must pay the seller at inception. However, the PUF can be negative, in which case  
25 the seller must make this payment up-front to the buyer (in addition to compensat-  
ing the buyer later in the event of default). (White, 2014).

27 The PUF can thus be considered to be the present value of the difference between  
the contractual coupon payments and the par spread the buyer would have been  
expected to pay instead under the prior convention over the CDS’ life (“Standard  
29 Corporate CDS Handbook,” Barclays Capital, February 2010, page 18). Given this  
equivalence between PUFs and par spreads, our following discussion of inferring  
the default probability associated with a CDS’ reference obligation from its par  
31 spread (hereafter “spread”) can be modified for standardized contracts following  
the Big Bang protocol to be based on the observed PUF rather than the par spread.

33 19. In practice, CDS premiums may be paid quarterly and default could occur  
any time during a year. If for instance, one assumed that default were to occur mid-  
35 year, then the calculations would be more complicated, and involve, in the event of  
default, accrued premium for six months, from the end of the previous year to the  
date of default, which the CDS buyer would have to pay to the seller upon default.  
37 Of course, this would be netted against the notional amount less the recovery rate  
the seller in turn would have to pay the buyer upon default (Hull, 2015). CDS fea-  
39 tures the “day convention” used to determine the timing of CDS-related cash flows  
change over time (White, 2014).

1 Hence, the calculation of the hazard rate from observed CDS market data too  
2 must change to reflect changes in contractual features. Further, CDS transactions in  
3 practice work somewhat differently from the hypothetical example discussed above  
4 given the PUF (Pay up-front) convention discussed earlier. CDS contracts now  
5 have a stated coupon and the buyer must pay the seller up-front for the present  
6 value of the difference between the par spread and the stated coupon (Hull, 2015,  
7 Chapter 15).

8 20. A “risk-averse” investor is one who, if faced with a choice between two risky  
9 investments with the same expected return, prefers the one with the lower risk.

10 21. In other words, to price a derivative, its cash flows are not directly estimated.  
11 Instead, it is assumed that the price of the underlying security (such as stock or  
12 bond) properly reflects the underlying security’s expected future cash flows, and  
13 risk-averse investors’ estimated probabilities associated with such cash flows. The  
14 derivative is then valued from the perspective of a derivative trader who takes posi-  
15 tions in two securities such as a stock and a derivative based on the stock to com-  
16 pletely eliminate risk. Since the trader faces no risk, in an efficient market world  
17 without arbitrage possibilities, the derivative investors would earn the risk-free rate  
18 of return. That is, the value of the derivative is assumed to equal its expected cash  
19 flows, measured using the risk-neutral probability of default, discounted by the risk-  
20 free rate of return. It follows that the default probability inferred from a derivatives  
21 price, using the same risk-neutral valuation model yields a risk-neutral probability  
22 estimate.

23 22. Solving the following equation:  $(1 - p^{\text{RN}}) \times \$1 \text{ million} = \$0.84 \text{ million}$ , yields  
24 the risk-neutral probability of default,  $p^{\text{RN}} = 16\%$ .

25 23. See Hull (2015) for a discussion of risk-neutral and real-world probabilities.

26 24. Berndt, Douglas, Duffie, Ferguson, and Schranz (2008) explain that “This  
27 ratio [of risk-neutral to actual default probabilities] may be viewed as the propor-  
28 tional premium for bearing default risk. For example, if this ratio is 2.0 (for a par-  
29 ticular firm, date, and maturity), then market-based insurance that pays one dollar in  
30 the event of default would be priced at roughly twice the expected discounted  
31 default loss.”

32 25. Berndt et al. (2008), Fig. 2.

33 26. Arora, Gandhi, and Longstaff (2012).

34 27. See Driessen (2005), Longstaff et al. (2005), and Berndt et al. (2008).

35 28. For example, as of January 27, 2015, we found such quotes from 11 dealers  
36 on Bloomberg related to a CDS contract with 5-year tenor which referenced Bank  
37 of America’s “senior unsecured” debt. The minimum and maximum “bids” across  
38 these dealers for the same CDS contract were, 69.18 and 71, respectively. The mini-  
39 mum and maximum “asks” across these dealers for the same CDS contract were, 73  
40 and 75, respectively.

41 29. SRO Published List issued by MarkitSERV on Wednesday, December 31,  
42 2014.

43 30. MarkitSERV is an electronic trade processing company created by Markit  
44 and The Depository Trust & Clearing Corporation in 2009 (<https://www.markit.com/product/markitserv>).

45 31. Most CDS contracts are standardized to facilitate trading and follow con-  
46 tractual definitions and reference “Standard Reference Obligations” according to

1 rules introduced by the International Swaps and Derivatives Association (ISDA) in  
2014. See ISDA, “2014 Credit Derivatives Definitions & Standard Reference  
3 Obligations” June 30, 2014.

32. SRO Published List issued by MarkitSERV on Wednesday, December 31,  
4 2014.

5 33. For example, Bank of America, one of the largest banks in the world, is not  
included in MarkitSERV’s SRO Published List as a standardized reference entity.  
6 Yet, we found CDS contracts that reference Bank of America’s senior and subordi-  
7 nated debt are currently traded. According to Bloomberg, three particular Bank of  
America senior bonds could be used as the reference obligation for the former CDS  
8 contract, while four other Bank of America subordinate bonds could be used as the  
reference obligation for a CDS contract referencing the bank’s subordinate debt.  
9 The menu of possible reference obligations are provided by MarkitSERV according  
10 to Bloomberg.

13 34. See HSBC Banks “5.844% Non-cumulative Step-up Perpetual Preferred  
Securities” dated October 31, 2003.

15 35. The SRO Published List is revised every quarter. Notably, the SRO identified  
for a particular reference entity is used as the reference debt obligation for CDS  
16 contracts of all tenors related to that entity. Hence, the remaining maturity of an  
SRO may be shorter (e.g., 1 year) than the CDS contract’s tenor (which could be 5  
17 years or more). In such cases, the SRO is substituted with a new SRO with longer  
remaining maturity. Specifically, when the remaining maturity of an SRO related to  
18 a CDS contract referencing an “M(M)R Financial Reference Entity” declines to  
less than 1 year, it is substituted by MarkitServe on the next quarter’s SRO  
19 Reference List. The substitute SRO selected is a debt obligation that was obviously  
issued by the same firm and has the same senior (senior or subordinate) as did the  
20 previous SRO. For non-M(M)R reference entities, an SRO must be substituted  
21 when its remaining maturity declines to 6 months or less. See “2014 Credit  
Derivatives Determinations Committees Rules”, ISDA, September 16, 2014.  
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32

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